

Using well-seismic mistie to update the velocity model^a

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ABSTRACT

We propose a method to aid in velocity model building based on misties between modeled synthetic seismograms from well log data and the seismic image. The method is based on the fact that when the migration velocity is inconsistent with the true migration velocity, there is a mistie between a modeled synthetic seismogram from well log data and the seismic image. The proposed approach uses local similarity to estimate the mistie at every sample along the synthetic seismogram and uses the result to update the migration velocity at the well location. The updated velocity information is interpolated along seismic structure using predictive painting to generate a new geologically consistent velocity model. We iteratively update the migration velocity model using only the seismic-well tie mistie. The results of our experiments with a simple layered model and an isotropic synthetic model indicate that the proposed workflow provides an effective method for integrating well log data in conventional velocity model building workflows.

INTRODUCTION

Well logs can be used to interpret geologic features at much higher resolution than that of the seismic data. Consequentially, well logs are often used to calibrate seismic images which have lower resolution but much higher spatial coverage to understand the distribution of subsurface rock properties (White and Simm, 2003). This calibration is referred to as a seismic-well tie, where reflectors from a well log modeled synthetic seismicogram are aligned with common reflectors in the seismic data. Any mis-ties between the modeled synthetic seismograms and seismic data are used to update the well's time to depth relationship (TDR) and are often related to inaccuracies in the seismic migration velocities (White, 1998).

In an attempt to reduce the mis-tie between well log information, which is taken as ground truth, and the seismic image, well log measurements are often injected into migration velocity model building to provide constraints in an otherwise non-unique problem (Bakulin et al., 2010). Morice et al. (2004) show that combining well log, borehole and surface seismic data can provide an understanding of seismic velocities, anisotropy, attenuation and interbed multiples which can aid in building a

velocity model consistent between all datasets. Egozi et al. (2006) show that mis-tie surfaces generated from multiple picks in multiple wells can be used to iteratively update a TTI velocity field thus driving the cumulative average mistie of all wells towards zero. Using well marker-related workflows in velocity model building removes or reduces nonuniqueness and may allow for simultaneous estimation of velocity and anisotropy parameters which can be used to constrain tomography problems that focus on flattening the residual moveout of seismic events (Woodward et al., 2008; Bakulin et al., 2010).

Although well marker-related workflows help integrate well log interpretations with seismic velocity model building; these methods are limited to updates related to discrete pre-selected well markers. Several methods have been proposed to automatically perform the seismic-well tie and provide a continuous mis-tie function along the entire length of the modeled synthetic seismogram. Some authors (Muñoz and Hale, 2012; Wu and Caumon, 2017) use dynamic time warping (DTW) (Berndt and Clifford, 1994; Hale, 2013) to automatically align real and synthetic seismograms. Herrera et al. (2014) show that local similarity (LSIM) (Fomel, 2007a) can be an alternative approach to successfully compute a seismic-well tie and compares the results with DTW. Bader et al. (2018) use LSIM to semi-automatically tie several wells to a 3D seismic dataset and provide a technique for cross validation to ensure consistency and accuracy of seismic-well ties. In each case, the mis-tie function is converted to an update applied to the velocity log.

In workflows where updates are not based on the tomographic principle, the velocity model update is dependent on the quality of the interpolation algorithm and horizon picks (Gupta et al., 2013). Several methods have been proposed to interpolate information along local seismic structures. Hale (2010) uses image guided blended neighbor interpolation (Hale, 2009) for seismic guided well log interpolation. Karimi et al. (2017) apply predictive painting (Fomel, 2010) to interpolate log data along seismic structures to generate accurate starting models for post stack inversion.

To understand and remove the inconsistencies between the migration velocity, well logs, migrated seismic image and modeled synthetic seismogram, we propose a method that uses LSIM to measure the mis-tie from the seismic-well tie and uses the result to update the migration velocity at the well log positions. A complete, updated, velocity model is then interpolated along seismic structures using predictive painting. We test our method on several synthetic datasets. The results indicate that the proposed workflow provides an effective method for incorporating well log data in velocity model building workflows.

THEORY

Seismic-well ties involve matching waveforms from a modeled synthetic seismogram with a nearby seismic trace (White and Simm, 2003). When comparing two datasets, our purpose is to estimate the warping function, S_k , required to align the synthetic

seismogram, h_k , with the seismic trace, r_k ,

$$r_k(t) \approx h_k(S_k(t)). \quad (1)$$

We can represent the warping function with time shifts, $g_k(t)$, as follows:

$$S_k(t) = t + g_k(t), \quad (2)$$

where the t denotes the original independent axis and $g_k(t)$ is the shifts required to match the datasets as defined in Equation 1. The LSIM method begins with the observation that the correlation coefficient only provides one number to describe the datasets in a defined window; however, we are interested in understanding the local changes in the datasets' similarity. Therefore, the LSIM method computes local similarity, which is a continuous function of time. The square of the correlation coefficient can be split into a product of two factors and posed as a regularized inversion where regularization operator is defined using shaping regularization and designed to enforce smoothness (Fomel, 2007a,b). From the similarity scan, we automatically pick the series of shifts along the entire length of the reference dataset that optimally aligns the two datasets (Fomel and Jin, 2009; Bader et al., 2017).

The relationship between the shifts estimated using LSIM and an updated velocity log assuming a TDR can be defined as:

$$T_0(z) = 2 \int_{z_{min}}^z \frac{d\xi}{v_0(\xi)}, \quad (3)$$

where T_0 is the initial TDR, z_{min} is the minimum depth at which sonic information is available, $v_0(\xi)$ is the initial, upscaled, P-wave velocity from sonic and $d\xi$ is the depth increment. From Equation 2, assuming an initial TDR, T_0 , we arrive at

$$S_{k,1}(T_0) = T_0 + g_{k,1}(T_0) \quad (4)$$

after one iteration of LSIM. We estimate a updated TDR by interpolating our shifts from time to depth

$$T_1(z) = T_0(z) + g_{k,1}(T_0(z)) \quad (5)$$

Using Equation 3, we relate the initial and updated velocity log to the initial and updated TDR,

$$\frac{dT_1(z)}{dz} \left(\frac{dT_0(z)}{dz} \right)^{-1} = \frac{v_0(z)}{v_1(z)} \quad (6)$$

Muñoz and Hale (2015), Herrera et al. (2014), and Bader et al. (2018) use Equation 6 to estimate an updated velocity log. Alternatively, if we assume that the migration velocity model is consistent with velocities from logs, we update the migration velocity at the well location based on the proportion of the updated well log velocity to the initial well log velocity:

$$v_{mig,1} = \frac{v_1(z)}{v_0(z)} v_{mig,0}. \quad (7)$$

We use predictive painting (Fomel, 2010) to spread the updated migration velocity, $v_{mig,1}$, from the wells throughout the seismic volume. We weight the interpolation based on the distance between the reference well and any location in the seismic dataset using radial basis functions (Karimi et al., 2017).

Using Equations 3–7, the migration velocity is iteratively updated using well tie updates. The seismic trace from the RTM depth image is stretched to time using the well log velocity profile and compared with the modeled synthetic seismogram from well logs. Figure 1 illustrates the workflow we use and is colored based on the data type used in each step.

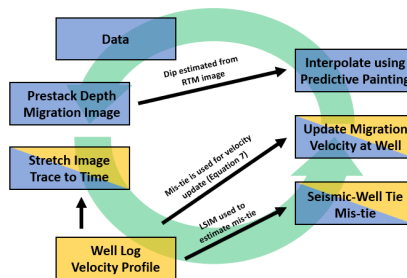


Figure 1: Workflow used in seismic-well tie velocity model updates. Blue indicates seismic data is used in the step. Yellow indicates well log data is used in the step. Black arrows indicate how the product of one step is used in a different step.

NUMERICAL EXAMPLES

We test the proposed approach on a simple layered and a more complex isotropic synthetic model. The simple layered model and isotropic synthetic model assume isotropic layers intersect vertical wells; reverse time migration (RTM) is performed to get a depth migration image.

Horizontally Layered Isotropic Example

We model data using the true velocity model shown in Figure 2a, and the migration velocity is shown in Figure 2b. Because each layer is perfectly horizontal, we anticipate that the incorrect migration velocity will cause a discrepancy between the seismic image layer interfaces and the true interfaces from the velocity model.

A seismic trace is extracted from the seismic image at location 1000m and compared against a modeled synthetic seismogram using a velocity ‘well log’ from the true velocity mode at 1000m. The seismic-well tie is automatically carried out using LSIM and a mis-tie function is estimated using the LSIM scan in Figure 3. The mis-tie is used to tie the synthetic to the seismic trace in Figure 4 indicating the mis-tie function properly related synthetic and seismic traces.

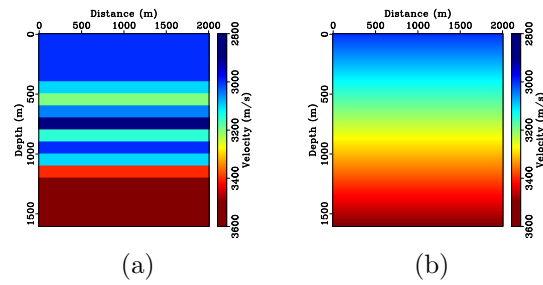


Figure 2: (a) True velocity model. (b) Initial migration velocity model. The velocity profile selected for the well tie update is located at 1000m. [smpl/vels,vel2](#)

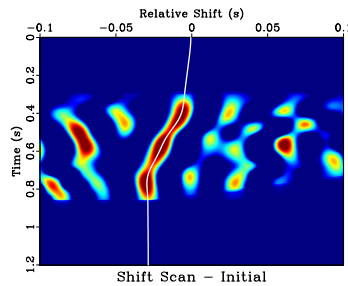


Figure 3: Similarity scan using the seismic trace at 1000m, stretched to time using the well log velocity, as the reference trace compared against the synthetic seismogram modeled from the velocity profile extracted at 1000m in Figure 2b. [smpl/scan2](#)

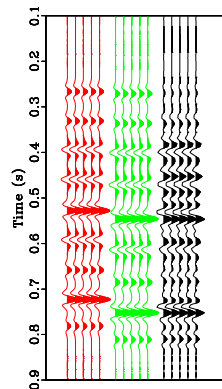


Figure 4: Initial synthetic seismogram (red). Synthetic seismogram stretched using the shifts estimated from LSIM scan in Figure 3 (green). Seismic trace extracted from RTM image stretched to time (black). [smpl/synthp2](#)

When working with the ‘final’ seismic image, the mis-tie can be converted to a velocity log update as shown in Figure 5a. Alternatively, we use Equation 7 to update the migration velocity as shown in Figure 5b. After ten iterations of well tie updates, we observe that the migration velocity is consistent with the well log velocity in Figure 5c. Note that the updated migration velocity section above 400m and below 1200 is inconsistent with the real velocity as well ties are only possible in between the first and last impedance contrast in the well log data.

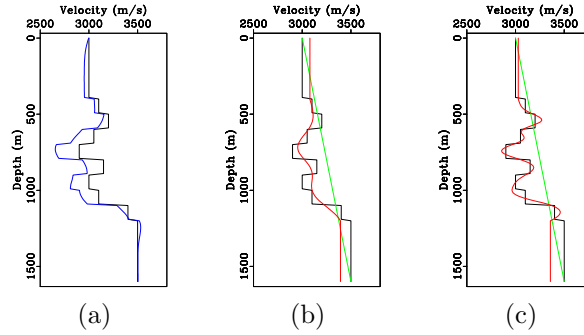


Figure 5: Well log velocity profile (black). (a) Common workflow of applying the mistie from the synthetic-well tie in Figure 4 to update velocity log (blue). (b) Proposed approach of using the mistie from the synthetic-well tie in Figure 4 to update initial migration velocity (green) at the well location after one iteration (red). (c) Migration velocity profile at the well location after 10 iterations of well tie updates (red) [smpl/ velupdate2,itr2,itrfi](#)

The simple layered model provides the understanding that in isotropic velocity models, the primary reason behind the mis-tie between well log modeled synthetics and seismic data is in the accuracy of the seismic migration velocities. Assuming that the entire mis-tie is related to incorrect vertical positioning of the reflector, the migration velocity model can be effectively updated using Equation 7.

Dipping Isotropic Example

In the simple layered model, we assumed that the entire mis-tie is related to the vertical positioning of the reflector. However, as pointed out by Bakulin et al. (2010), solving the mis-tie equations along the axis of the well may result in biased estimates of velocities in the presence of dipping layers. To account for biased estimates of migration velocity updates due to dipping layers, we propose to migrate the data several times per iteration using perturbed velocity models. We use four percent increments to perturb the model. We then perform the seismic-well tie using each of the resulting seismic images and convert the mis-tie to a migration velocity update. We estimate the migration velocity update as the semblance weighted average of the velocity updates from each mis-tie.

We model data using the true velocity model shown in Figure 6a, and the initial migration velocities are shown Figure 7a. We use a velocity profile from five ‘wells’ located at 1000m, 2000m, 3000m, 4000m, and 5000m. With each iteration, we assume the velocity of the layer between 0m and 400m is known.

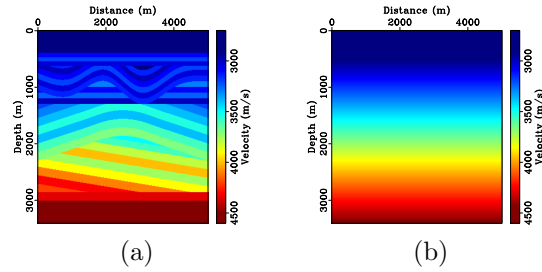


Figure 6: (a) True velocity model. (b) One of the initial migration velocity model perturbations for the first iteration. The wells selected for well tie updates are located at 1000m, 2000m, 3000m, 4000m, and 5000m. [iso/ vel,vel2-2](#)

The seismic traces at locations 1000m, 2000m, 3000m, 4000m, and 5000m from each seismic image are stretched to time using the true well log velocity and the misties is estimated using local similarity. Using Equation 7, we update the migration velocity at each well location. The results of migration velocity updates at well location 3000m for the five initial migration velocity models shown in Figure 7a are shown in Figure 7b. We spread the information along seismic structures using predictive painting weighted by radial basis functions to generate a new geologically consistent migration velocity model.

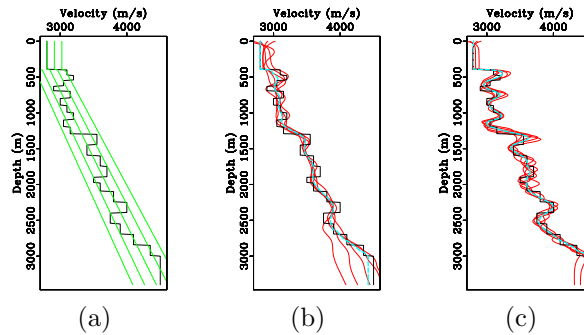


Figure 7: True velocity model at well location 3000m (black). (a) Starting migration velocity models with a linearly increasing velocity gradient (green). (b) Migration velocity updates from well tie updates based on the mistie between the synthetic seismogram modeled from the well log profile and the seismic image migrated from the five perturbed velocity models (red). Semblance weighted average of the five migration velocity updates (cyan), this result is used for interpolation of the next migration velocity model. (c) Results after six iterations of well tie updates.

[iso/ vels2,wellvel2-3,wellvel7-3](#)

We iteratively update the migration velocity model by generating five perturbed migration velocity models at each iteration and estimating the semblance weighted average of the velocity updates from each mis-tie. Each iteration, we reduce the perturbation of the migration velocity models and the smoothing in local similarity. Results after six iterations of well tie updates at well location 3000m are shown in Figure 7c. We observe that the semblance weighted average of the velocity updates at this location fits well with the real well log velocity. The migration velocity model after six iterations is shown in Figure 8b and is reasonably consistent with the real velocity model in Figure 6a.

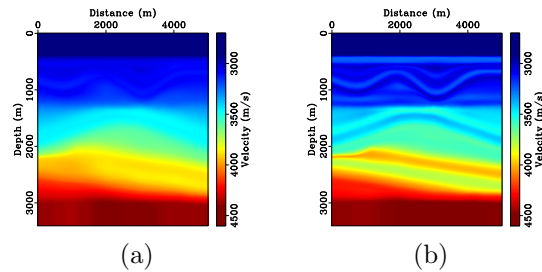


Figure 8: (a) Migration velocity model after one iteration and (b) six iterations of well tie updates and weighted interpolation of the updated velocity profile from the wells using predictive painting. [iso/ vel3,vel8](#)

Figure 9c is the final depth migrated seismic image using the velocity model in Figure 8b. This result is compared against Figure 9d, the depth migrated seismic image using the real velocity model. Differences in the velocity models result in small differences in reflector positioning.

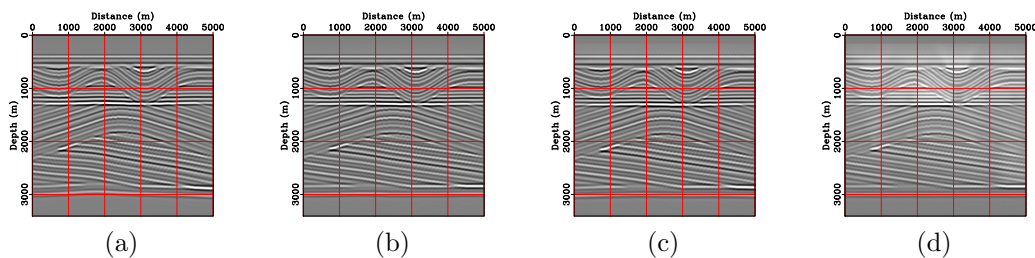


Figure 9: (a) Initial RTM image using the migration velocity perturbation shown in Figure 6b. (b) RTM image using the migration velocity perturbation shown in Figure 8a. (c) Final RTM image using the migration velocity shown in Figure 8b after six iterations. (d) RTM image using the true migration velocity in Figure 6a.

[iso/ rtm2-2,rtm3-2,rtm8,rtm](#)

CONCLUSIONS

We present an approach to aid in velocity model building using misties between modeled synthetic seismograms from well log data and the seismic image. The proposed approach provides a unique method for integrating well log data in conventional velocity model building workflows. The proposed workflow is not a substitute for conventional velocity analysis, but it may help to reduce nonuniqueness in areas of complex stratigraphy or anisotropy. In our approach, local similarity is used to estimate the mistie at every sample along the synthetic seismogram and uses the result to update the migration velocity at the well location. Because inaccuracies in the migration velocity are directly related to the mis-tie and observed in seismic-well ties, this information can be used to update the migration velocity at the well location and be spread throughout the model using predictive painting. Iteratively updating the migration velocity using the proposed workflow results in a high-resolution migration model that is consistent with well log data.

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